

Data Structures – CST 201

Module - 2

Syllabus

- Searching
 - Linear Search
 - Binary Search
- Polynomial representation using Arrays
- Sparse matrix
- Stacks
- Queues
 - Circular Queues
 - Double Ended Queues
 - Priority Queues
- **Evaluation of Expressions**

APPLICATIONS OF STACK

1. Evaluation of arithmetic expressions
2. Implementation of Recursion
3. String reversal

APPLICATIONS OF STACK

1. **Evaluation of arithmetic expressions**
2. Implementation of Recursion
3. String reversal

Evaluation of arithmetic expressions

- An arithmetic expression consist of operands and operators
- Operands are variables or constants
- Operators are various types such as arithmetic unary and binary operators and Boolean operators
- Parenthesis are also used
- Eg1: $a+b*c/d$
- Eg2: $(a+((b*c)/d))$

Evaluation of arithmetic expressions

- Problem to evaluate these expression is the order of evaluation.
- We can assign each operator a precedence and associativity

Operator	Precedence	Associativity
+, - (unary)	1	
^	2	Right to left
*, /	3	Left to right
+, - (binary)	4	Left to right

EXPRESSIONS

- The way to write arithmetic expression is known as notation
- Arithmetic expressions can be written in 3 different ways
 - Infix notation
 - Postfix(Polish) notation
 - Prefix(Reverse-Polish) notation

Evaluation of arithmetic expressions

- Evaluation of expression is a two step process
 1. Convert given infix expression into postfix/prefix expression
 2. Evaluate the postfix/prefix expression
- In each procedure stack is the main data structure that we used to accomplish its task

INFIX NOTATION

- Operators are written between the operands they act on.
- Ex: $5+2$
- In infix notation, parentheses surrounding groups of operands and operators are necessary to indicate the intended order in which operations are to be performed.
- In the absence of parentheses, certain precedence rules determine the order of operations.

PREFIX NOTATION

- Operator precede the Operands
- Parentheses are not used
- Ex: +52

$$((A + ((B \wedge C) - D)) * (E - (A / C)))$$

$$((A + ((B \wedge C) - D)) * (E - (A / C)))$$

$$((A + ((B \wedge C) - D)) * (E - (A / C)))$$

$\wedge B C$

$$((A + (^B C - D)) * (E - (A / C)))$$

$$((A + (^B C - D)) * (E - (A / C)))$$

$$((A + (\wedge B C - D)) * (E - (A / C)))$$

$-\wedge B C D$

$$((A + - ^ B C D) * (E - (A / C)))$$

$$((A + - ^ B C D) * (E - (A / C)))$$

$((A + - ^ B C D) * (E - (A / C)))$

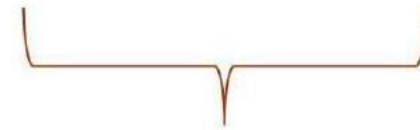


$+ A - ^ B C D$

(+ A - ^ B C D * (E - (A / C)))

$(+ A - ^{\wedge} B C D * (E - (A / C)))$

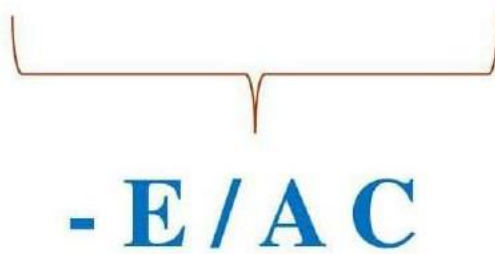
(+ A - ^ B C D * (E - (A / C)))



/AC

$(+ A - ^{\wedge} B C D * (E - / A C))$

(+ A - ^ B C D * (E - / A C))

$$(+ A - ^{\wedge} B C D * (E - / A C))$$


The image shows a mathematical expression: $(+ A - ^{\wedge} B C D * (E - / A C))$. A brown bracket is drawn under the sub-expression $(E - / A C)$. Below the bracket, the text $- E / A C$ is written in blue.

(+ A - ^ B C D * - E / A C)

(+ A - ^ B C D * - E / A C)

(+ A - ^ B C D * - E / A C)

* + A - ^ B C D - E / A C

*** + A - ^ B C D - E / A C**

POSTFIX NOTATION

- Operands precede the operator
- Parentheses are not used
- Ex: $52+$

$$((A + ((B \wedge C) - D)) * (E - (A / C)))$$

$$((A + ((B \wedge C) - D)) * (E - (A / C)))$$

$$((A + ((B \wedge C) - D)) * (E - (A / C)))$$

$B \wedge C$

$$((A + (BC^{\wedge} - D)) * (E - (A/C)))$$

$$((A + (BC^{\wedge} - D)) * (E - (A/C)))$$

$$((A + (BC^{\wedge} - D)) * (E - (A/C)))$$

$$BC^{\wedge}D -$$

$$((A + B C ^ D -) * (E - (A / C)))$$


$$((A + B C^{\wedge} D -) * (E - (A / C)))$$

$((A + B C ^ D -) * (E - (A / C)))$

$A B C ^ D - +$

(A B C ^ D - + * (E - (A / C)))

(A B C ^ D - + * (E - (A / C)))

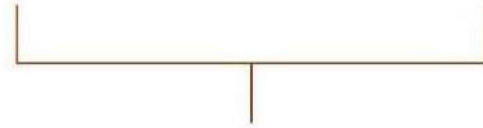
$$(A B C ^ { \wedge } D - + * (E - (A / C)))$$


The diagram illustrates the evaluation of a sub-expression within a larger mathematical formula. The expression is $(A B C ^ { \wedge } D - + * (E - (A / C)))$. A brown bracket is drawn under the sub-expression (A / C) . Below the bracket, the text $A C /$ is written in blue, indicating the result of the division operation.

(A B C ^ D - + * (E - A C /))

(A B C ^ D - + * (E - A C /))

(A B C ^ D - + * (E - A C /))



E A C / -

(A B C ^ D - + * **E A C / -**)

(A B C ^ D - + * E A C / -)

(A B C ^ D - + * E A C / -)

A B C ^ D - + E A C / - *

A B C ^ D - + E A C / - *

Infix Expression	Prefix Expression	Postfix Expression
$A+B$	$+AB$	$AB+$
$A+B-C$	$--+ABC$	$AB+C-$
$(A+B)*(C-D)$	$*+AB-CD$	$AB+CD-*$
$((A+B)*C)-D$	$-*+ABCD$	$AB+C*D-$
$A+B*C-D+E/F/(G+H)$	$+-A*BCD//EF+GH$	$ABC*+D-EF/GH+//+$
$((A+B)*C-(D-E))/(F+G)$	$/-*+ABC-DE+FG$	$AB+C*DE--FG+//$
$A-B/(C*D/E)$	$-A/B/*CDE$	$ABCD*E//-$


INFIX TO POSTFIX CONVERSION ALGORITHM

$$A - B / (C * D / E)$$

6	
5	
4	
3	
2	
1	
0	

S

Postfix Expression:


$$\mathbf{A} - \mathbf{B} / (\mathbf{C} * \mathbf{D} / \mathbf{E})$$


6	
5	
4	
3	
2	
1	
0	

S

Postfix Expression:

A - B / (C * D / E)




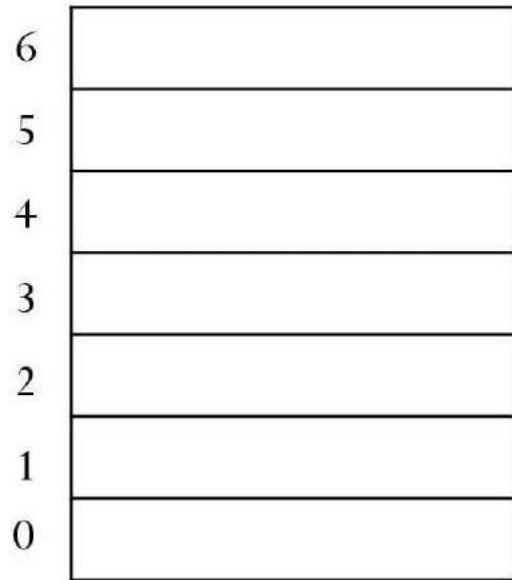
6	
5	
4	
3	
2	
1	
0	

S

Postfix Expression:

A


$$A - B / (C * D / E)$$




S

Postfix Expression:

A


$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	
1	
0	-

S

Postfix Expression:

A


$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	
1	
0	-

S

Postfix Expression:

A

$$A - B / (C * D / E)$$


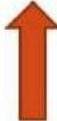
6	
5	
4	
3	
2	
1	
0	-

S

Postfix Expression:

A B

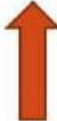
A - B / (C * D / E)



6	
5	
4	
3	
2	
1	
0	-

S


Postfix Expression:
A B

$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	
1	/
0	-

S

Postfix Expression:
A B


$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	
1	/
0	-

S

Postfix Expression:
A B

A - B / (C * D / E)




6	
5	
4	
3	
2	(
1	/
0	-

S

Postfix Expression:


A B

$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	(
1	/
0	-

S


Postfix Expression:
A B

$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	(
1	/
0	-

S

Postfix Expression:
A B C

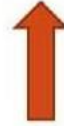
$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	(
1	/
0	-

S

Postfix Expression:
A B C

A - B / (C * D / E)




6	
5	
4	
3	*
2	(
1	/
0	-

S

Postfix Expression:


A B C

$$A - B / (C * D / E)$$


6	
5	
4	
3	*
2	(
1	/
0	-

S


Postfix Expression:
A B C

$$A - B / (C * D / E)$$


6	
5	
4	
3	*
2	(
1	/
0	-

S


Postfix Expression:
A B C D

$$A - B / (C * D / E)$$


6	
5	
4	
3	*
2	(
1	/
0	-

S


Postfix Expression:
A B C D

$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	(
1	/
0	-

S


Postfix Expression:
A B C D *

$$A - B / (C * D / E)$$


6	
5	
4	
3	/
2	(
1	/
0	-

S


Postfix Expression:
A B C D *

$$A - B / (C * D / E)$$


6	
5	
4	
3	/
2	(
1	/
0	-

S

Postfix Expression:
A B C D *


$$A - B / (C * D / E)$$


6	
5	
4	
3	/
2	(
1	/
0	-

S

Postfix Expression:
A B C D * E


A - B / (C * D / E)



6	
5	
4	
3	/
2	(
1	/
0	-

S

Postfix Expression:
A B C D * E


$$A - B / (C * D / E)$$


6	
5	
4	
3	/
2	(
1	/
0	-

S

Postfix Expression:
A B C D * E


A - B / (C * D / E)



6	
5	
4	
3	
2	(
1	/
0	-

S


Postfix Expression:
A B C D * E /

$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	
1	/
0	-

S

Postfix Expression:
A B C D * E /


$$A - B / (C * D / E)$$


6	
5	
4	
3	
2	
1	
0	-

S

Postfix Expression:
A B C D * E //

A - B / (C * D / E)



6	
5	
4	
3	
2	
1	
0	

S

Postfix Expression:
A B C D * E / / -

INFIX TO POSTFIX -ALGORITHM

Algorithm infix_to_postfix(A, P, S)

```
{  
  i=0  
  while A[i]!='\0' do  
  {  
    if A[i] is an operand then  
      ENQUEUE A[i] to P  
    else if A[i] = '(' then  
      PUSH A[i] to S  
    else if A[i] = ')' then  
      Repeatedly POP elements from S until the popped item is '('  
      ENQUEUE all these popped items into P except '('  
  }  
}
```

else

```
{ x=A[i]          y=S[top]
```

```
  if top=-1 or y='(' then
```

```
    PUSH x in to S
```

```
  else
```

```
    { while precedence(x)<=precedence(y) do
```

```
      { POP an item from S and ENQUEUE it in P
```

```
        y=S[top]
```

```
        if top=-1 or y='(' then          break
```

```
      }
```

```
      PUSH x in to S
```

```
    }
```

```
  }
```

```
}
```

Repeatedly POP remaining elements from S and ENQUEUE it in P

Print P

```
}
```

INFIX TO PREFIX CONVERSION ALGORITHM

$$\mathbf{A - B / (C * D / E)}$$

A - B / (C * D / E)

Reverse the string:) E / D * C (/ B - A

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A

6	
5	
4	
3	
2	
1	
0	

S

Prefix Expression:

Reverse the string:

A - B / (C * D / E)

) E / D * C (/ B - A
↑

6	
5	
4	
3	
2	
1	
0	

S

Prefix Expression:

Reverse the string:

A - B / (C * D / E)

) E / D * C (/ B - A
↑

6	
5	
4	
3	
2	
1	
0)

S

Prefix Expression:

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A
↑

6	
5	
4	
3	
2	
1	
0)

S

Prefix Expression:

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A
↑

6	
5	
4	
3	
2	
1	
0)

S

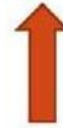
Prefix Expression:

E

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	
0)

S

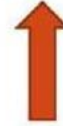
Prefix Expression:

E

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	/
0)

S


Prefix Expression:

E

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	/
0)

S

Prefix Expression:

E

Reverse the string:

A - B / (C * D / E)

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	/
0)

S

Prefix Expression:

E D

Reverse the string:

A - B / (C * D / E)

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	/
0)

S

Prefix Expression:

E D

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	*
1	/
0)

S


Prefix Expression:

E D

Reverse the string:

A - B / (C * D / E)

) E / D * C (/ B - A



6	
5	
4	
3	
2	*
1	/
0)

S


Prefix Expression:

E D

Reverse the string:

A - B / (C * D / E)

) E / D * C (/ B - A



6	
5	
4	
3	
2	*
1	/
0)

S

Prefix Expression:

E D C

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	*
1	/
0)

S

Prefix Expression:

E D C

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	/
0)

S

Prefix Expression:

E D C *

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	
0)

S

Prefix Expression:

E D C * /

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	
0	

S

Prefix Expression:

E D C * /

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	
0	

S

Prefix Expression:

E D C * /

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	
0	/

S

Prefix Expression:

E D C * /

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A
↑

6	
5	
4	
3	
2	
1	
0	/

S

Prefix Expression:

E D C * /

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A
↑

6	
5	
4	
3	
2	
1	
0	/

S

Prefix Expression:

E D C * / B

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	
0	/

S

Prefix Expression:

E D C * / B

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	
0	

S

Prefix Expression:

E D C * / B /

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	
0	-

S

Prefix Expression:

E D C * / B /

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A



6	
5	
4	
3	
2	
1	
0	-

S

Prefix Expression:

E D C * / B /

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A
↑

6	
5	
4	
3	
2	
1	
0	-

S

Prefix Expression:

E D C * / B / A

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A
↑

6	
5	
4	
3	
2	
1	
0	

S

Prefix Expression:

E D C * / B / A -

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A

6	
5	
4	
3	
2	
1	
0	

S

Prefix Expression:

E D C * / B / A -

Reverse the above Expression:

A - B / (C * D / E)

Reverse the string:

) E / D * C (/ B - A

6	
5	
4	
3	
2	
1	
0	

S

Prefix Expression:

E D C * / B / A -

Reverse the above Expression:

- A / B / * C D E

INFIX TO PREFIX -ALGORITHM

Algorithm infix_to_prefix(A, P, S)

{ Reverse A and place it in R

i=0

while R[i]!='\0' do

{

if R[i] is an operand then

ENQUEUE R[i] to P

else if R[i] = ')' then

PUSH R[i] to S

else if R[i] = '(' then

Repeatedly POP elements from S until the popped item is ')'

ENQUEUE all these popped items into P except ')'

else

```
{ x=R[i]          y=S[top]
```

```
  if top=-1 or y=')' then
```

```
    PUSH x in to S
```

```
  else
```

```
  { while precedence(x)<precedence(y) do
```

```
    { POP an item from S and ENQUEUE it in P
```

```
      y=S[top]
```

```
      if top=-1 or y=')' then          break
```

```
    }
```

```
    PUSH x in to S
```

```
  }
```

```
}
```

```
}
```

Repeatedly POP remaining elements from S and ENQUEUE it in P

Reverse P and Print it

```
}
```

POSTFIX EXPRESSION EVALUATION - ALGORITHM

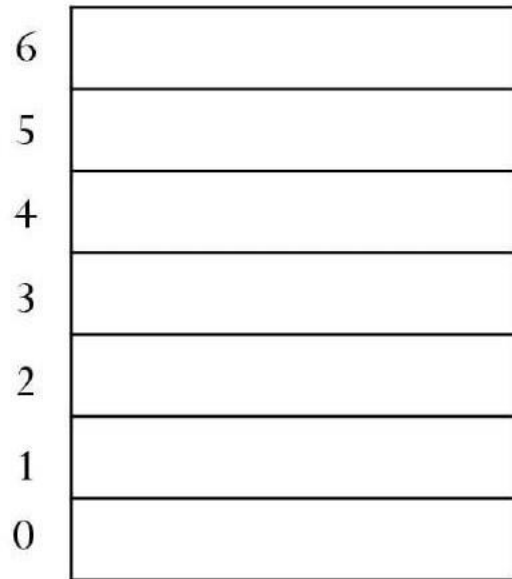
Infix Expression : $10 - 500 / (20 * 2 / 4)$

Infix Expression : **10 – 500 / (20 * 2 / 4)**

Postfix Expression : **10 500 20 2 * 4 / / -**

Infix Expression : **10 – 500 / (20 * 2 / 4)**

Postfix Expression : **10 500 20 2 * 4 / / -**



S

Infix Expression : **10 – 500 / (20 * 2 / 4)**

Postfix Expression : **10 500 20 2 * 4 / / -**



6	
5	
4	
3	
2	
1	
0	

S

Infix Expression : **10 – 500 / (20 * 2 / 4)**

Postfix Expression : **10 500 20 2 * 4 / / -**



6	
5	
4	
3	
2	
1	
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10 \mathbf{500} 20 2 * 4 / / -$



6	
5	
4	
3	
2	
1	
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10 \mathbf{500} 20 2 * 4 / / -$



6	
5	
4	
3	
2	
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ *\ 4\ /\ / -$



6	
5	
4	
3	
2	
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	20
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4 \ / \ / \ -$



6	
5	
4	
3	
2	20
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ *\ 4\ /\ / -$



6	
5	
4	
3	2
2	20
1	500
0	10

S

Infix Expression : **10 – 500 / (20 * 2 / 4)**

Postfix Expression : **10 500 20 2 * 4 / / -**



6	
5	
4	
3	2
2	20
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	20
1	500
0	10

S

* 2

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	
1	500
0	10

S

$20 * 2$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	
1	500
0	10

S

$$20 * 2 = 40$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	40
1	500
0	10

S

$$20 * 2 = 40$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	40
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / -$



6	
5	
4	
3	4
2	40
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	4
2	40
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	40
1	500
0	10

S

/ 4

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	
1	500
0	10

S

40 / 4

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	
1	500
0	10

S

$$40 / 4 = 10$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	10
1	500
0	10

S

$$40 / 4 = 10$$

Infix Expression : **10 – 500 / (20 * 2 / 4)**

Postfix Expression : **10 500 20 2 * 4 / / -**



6	
5	
4	
3	
2	10
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ *\ 4\ /\ / -$



6	
5	
4	
3	
2	
1	500
0	10

S

/ 10

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	
1	
0	10

S

500 / 10

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



6	
5	
4	
3	
2	
1	
0	10

S

$$500 / 10 = 50$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ * \ 4\ /\ / \ -$



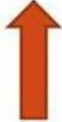
6	
5	
4	
3	
2	
1	50
0	10

S

$$500 / 10 = 50$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ *\ 4\ /\ / -$



6	
5	
4	
3	
2	
1	50
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ *\ 4\ /\ / -$



6	
5	
4	
3	
2	
1	
0	10

S

- 50

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ *\ 4\ /\ / -$



6	
5	
4	
3	
2	
1	
0	

S

10 - 50

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ *\ 4\ /\ / -$



6	
5	
4	
3	
2	
1	
0	

S

$$10 - 50 = -40$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ *\ 4\ /\ / -$



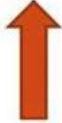
6	
5	
4	
3	
2	
1	
0	-40

S

$$10 - 50 = -40$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $10\ 500\ 20\ 2\ *\ 4\ /\ / -$



6	
5	
4	
3	
2	
1	
0	-40

S

POSTFIX EVALUATION - ALGORITHM

Algorithm postfix_eval(P)

```
{   for i=0 to length(P)-1 do
    {   if P[i] is an operand then
        PUSH P[i] to S
      else if P[i] is an operator then
        {   op2=POP()
            op1=POP()
            result = op1 P[i] op2
            PUSH result in to S
          }
      }
    }
  Print S[0]
}
```

PREFIX EXPRESSION EVALUATION - ALGORITHM

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Infix Expression : **10 – 500 / (20 * 2 / 4)**

Postfix Expression : **- 10 / 500 / * 20 2 4**

Infix Expression : $10 - 500 / (20 * 2 / 4)$

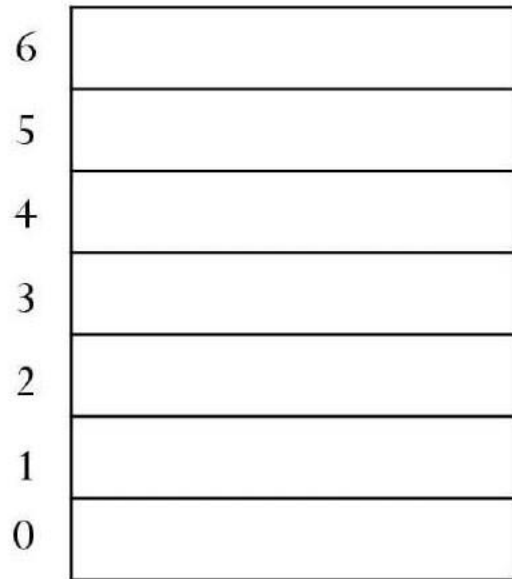
Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	4

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 \mathbf{2} 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	4

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 \mathbf{2} 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	2
0	4

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	2
0	4

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	20
1	2
0	4

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	20
1	2
0	4

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	2
0	4

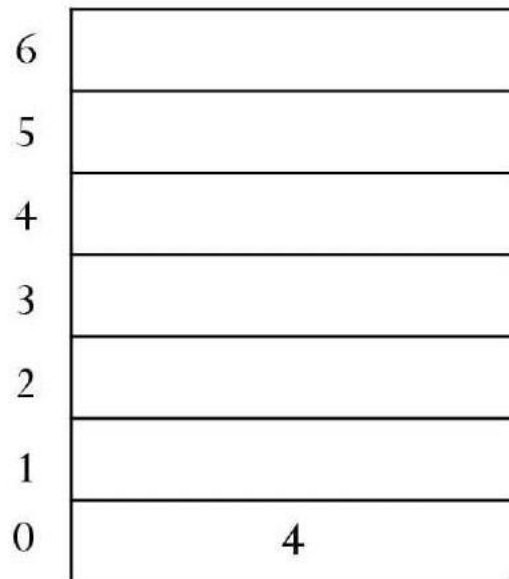
S

20 *

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



S

$20 * 2$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	4

S

$$20 * 2 = 40$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	40
0	4

S

$$20 * 2 = 40$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	40
0	4

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	4

S

40 /

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	

S

40 / 4

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	

S

$$40 / 4 = 10$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	10

S

$$40 / 4 = 10$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	500
0	10

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	10

S

500 /

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	

S

500 / 10

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	

S

$$500 / 10 = 50$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	50

S

$$500 / 10 = 50$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$

6	
5	
4	
3	
2	
1	
0	50

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$

6	
5	
4	
3	
2	
1	10
0	50

S

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$

6	
5	
4	
3	
2	
1	
0	50

S

10 -

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$

6	
5	
4	
3	
2	
1	
0	

S

10 - 50

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$



6	
5	
4	
3	
2	
1	
0	

S

$$10 - 50 = -40$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$

6	
5	
4	
3	
2	
1	
0	-40

S

$$10 - 50 = -40$$

Infix Expression : $10 - 500 / (20 * 2 / 4)$

Postfix Expression : $- 10 / 500 / * 20 2 4$

Reverse the Expression: $4 2 20 * / 500 / 10 -$

6	
5	
4	
3	
2	
1	
0	-40

S

PREFIX EVALUATION - ALGORITHM

Algorithm prefix_eval(P)

```
{   for i= length(P)-1 to 0 do
    {   if P[i] is an operand then
        PUSH P[i] to S
      else if P[i] is an operator then
        {   op1=POP()
            op2=POP()
            result = op1 P[i] op2
            PUSH result in to S
          }
      }
    }
  Print S[0]
}
```

APPLICATIONS OF STACK

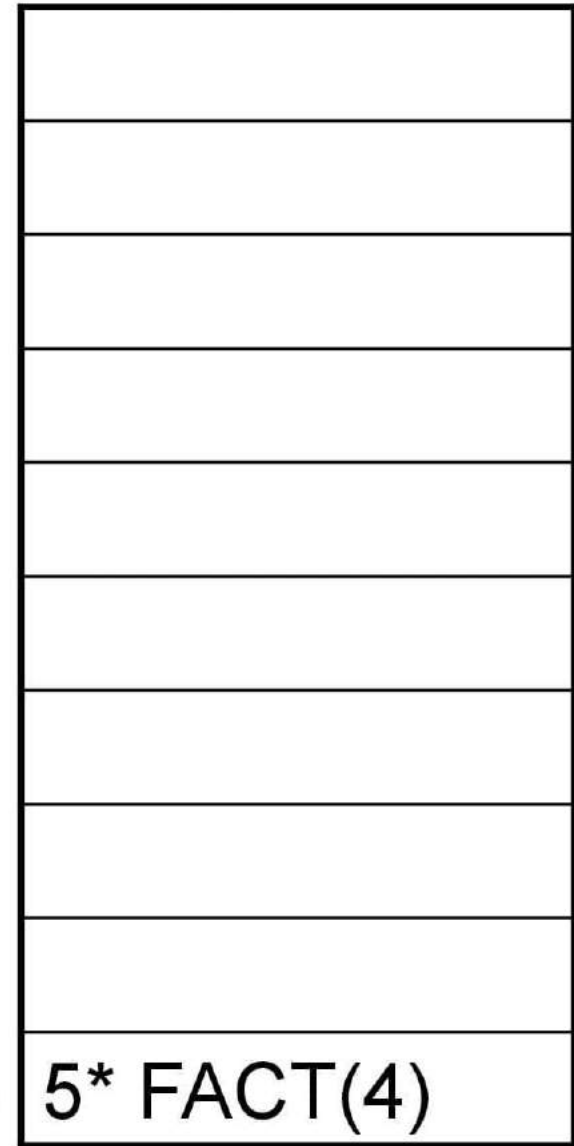
1. Evaluation of arithmetic expressions
2. **Implementation of Recursion**
3. String reversal

Program to find the factorial of a number using recursion

```
int FACT(int n)
{
    if (n == 0 || n == 1)
        return 1;
    else
        return n * FACT(n-1);
}
```


$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

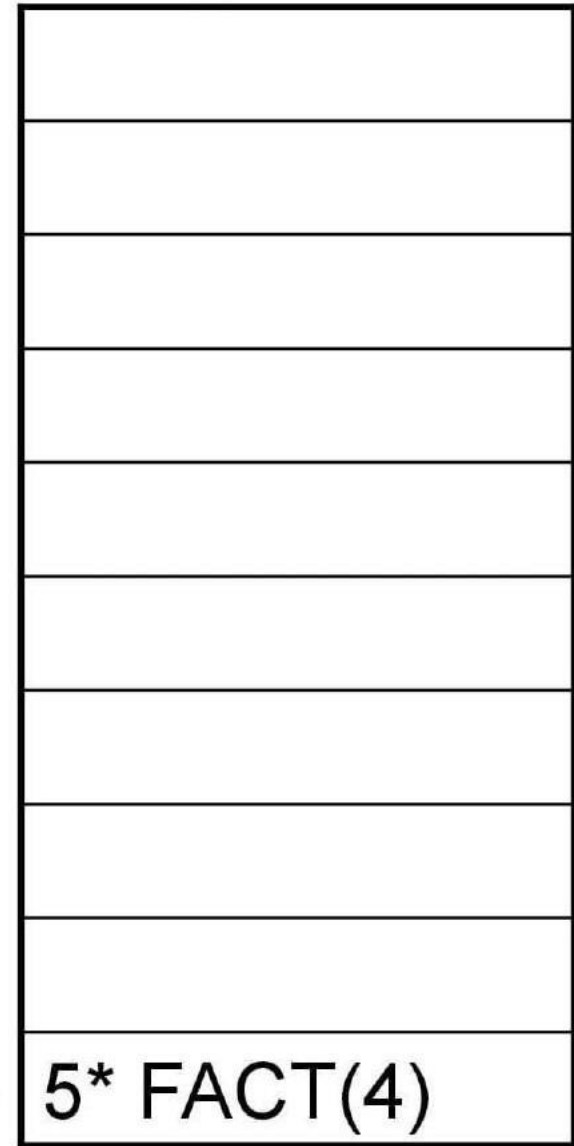
$$\text{FACT}(5) = 5 * \text{FACT}(4)$$



FACT(5) →

5* FACT(4)

$$\text{FACT}(5) = 5 * \text{FACT}(4)$$
$$= 4 * \text{FACT}(3)$$



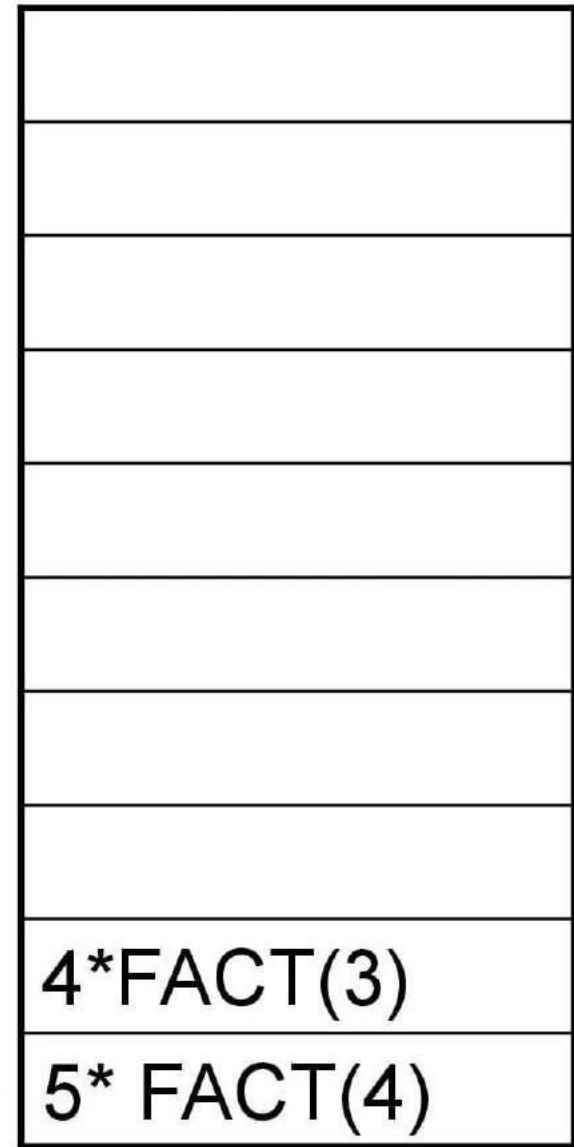
FACT(5) →

5* FACT(4)

$$\begin{aligned} \text{FACT}(5) &= 5 * \text{FACT}(4) \\ &= 4 * \text{FACT}(3) \end{aligned}$$

FACT(4) →

FACT(5) →



$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

FACT(4) →

4 * FACT(3)

FACT(5) →

5 * FACT(4)

$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

FACT(3) →

3 * FACT(2)

FACT(4) →

4 * FACT(3)

FACT(5) →

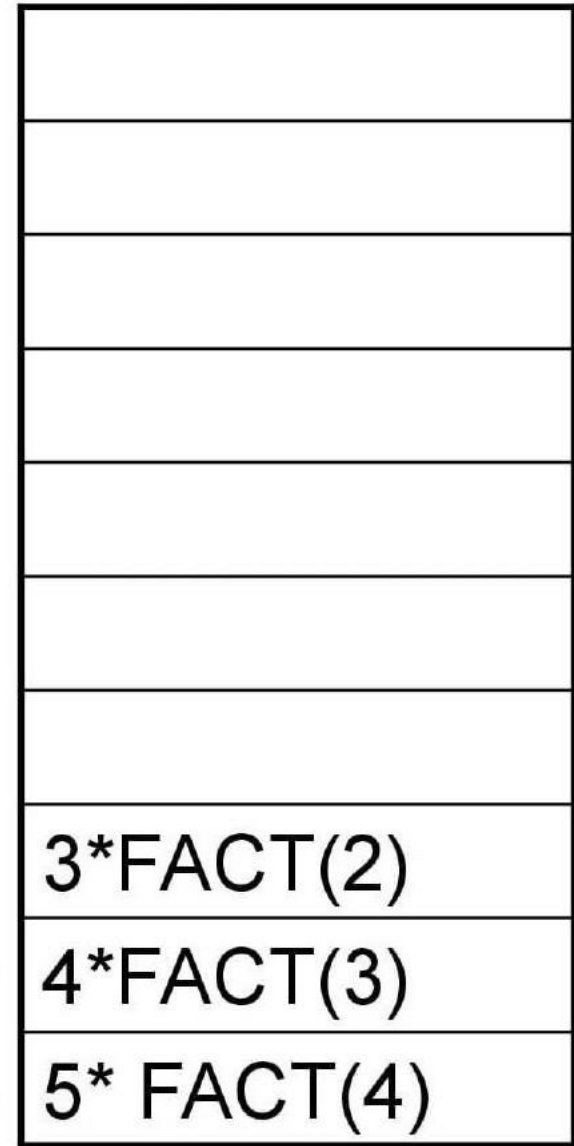
5 * FACT(4)

$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

$$= 2 * \text{FACT}(1)$$



FACT(3) →

3*FACT(2)

FACT(4) →

4*FACT(3)

FACT(5) →

5* FACT(4)

$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

$$= 2 * \text{FACT}(1)$$

FACT(2) →

2*FACT(1)

FACT(3) →

3*FACT(2)

FACT(4) →

4*FACT(3)

FACT(5) →

5*FACT(4)

$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

$$= 2 * \text{FACT}(1)$$

$$= 1$$

FACT(2) →

2*FACT(1)

FACT(3) →

3*FACT(2)

FACT(4) →

4*FACT(3)

FACT(5) →

5*FACT(4)

$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

$$= 2 * \text{FACT}(1)$$

$$= 1$$

FACT(2) →

2*1

FACT(3) →

3*FACT(2)

FACT(4) →

4*FACT(3)

FACT(5) →

5* FACT(4)

$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

$$= 2 * \text{FACT}(1)$$

$$= 1$$

FACT(2) →

2

FACT(3) →

3 * FACT(2)

FACT(4) →

4 * FACT(3)

FACT(5) →

5 * FACT(4)

$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

$$= 2 * \text{FACT}(1)$$

$$= 1$$

FACT(3) →

3*2

FACT(4) →

4*FACT(3)

FACT(5) →

5* FACT(4)

$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

$$= 2 * \text{FACT}(1)$$

$$= 1$$

FACT(3) →

FACT(4) →

FACT(5) →

6
4 * FACT(3)
5 * FACT(4)

$$\begin{aligned} \text{FACT}(5) &= 5 * \text{FACT}(4) \\ &= 4 * \text{FACT}(3) \\ &= 3 * \text{FACT}(2) \\ &= 2 * \text{FACT}(1) \\ &= 1 \end{aligned}$$

FACT(4) 

FACT(5) 

24
5* FACT(4)

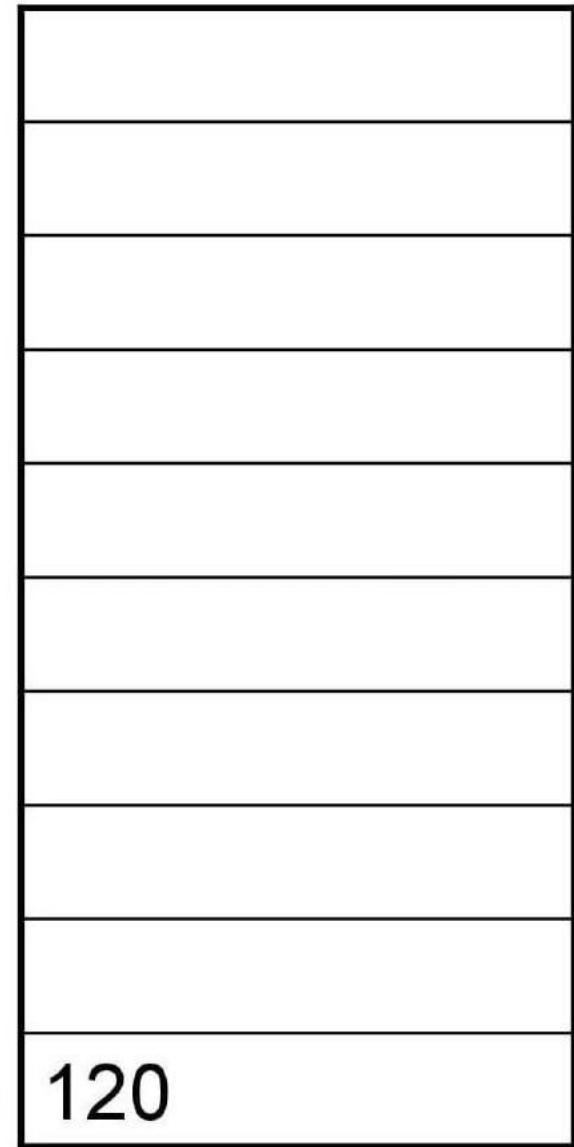
$$\text{FACT}(5) = 5 * \text{FACT}(4)$$

$$= 4 * \text{FACT}(3)$$

$$= 3 * \text{FACT}(2)$$

$$= 2 * \text{FACT}(1)$$

$$= 1$$



FACT(5) →

120

APPLICATIONS OF STACK

1. Evaluation of arithmetic expressions
2. Implementation of Recursion
3. **String reversal**

HELLO



HELLO

